Let $G$ be a group and $V$ be a representation of $G$. Define

$$ V_{g} := \{ v \in V | g \cdot v = \lambda g v \} $$

for any $g \in G$, where $\lambda g$ is the character of $g$. These subspaces are called the conjugacy classes.